## Design using intuition and logic

Optimisation, Graphical Models, Protein Design

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## SAT

- Canonical NP-complete problem (Cook theorem)
- A set $X$ of Boolean variables
- A set $C$ of clauses (disjunction of litterals: a variable or its negation)
- $\exists$ ? a labelling of $X$ such that all $C$ is true

SAT solvers find a solution or provide a proof that none exists

- Major impact on digital circuit verification (PSPACE-complete),...
- Theorem proving (recent proof on Pythagorean Triangles ${ }^{9,10}$ )
- Millions of variables, 10 s of millions of clauses

A lot of empirical work

- Lots of real problems (random problems are different)
- Competitions with Open Source software


## Main elected ingredients

- Massive problem reformulation using local inference (Unit Propagation, fast data-structures)
- If insufficient, make assumptions (tree search)
- Make non naive assumptions (adaptative variable ordering, learned during search)
- Conflict analysis (clause learning following inconsistent assumptions)
- Restarts,...


## Constraint network ( $X, C$ )

Joint feasibility distribution

- a sequence $X$ of variables $x_{i}$, finite domain $D_{i}$
- a set $C$ of constraints
- $c_{S} \in C$ involves variables in $S \subseteq X$
boolean functions table, clause,...

$$
\prod_{i \in S} D_{i} \rightarrow\{t, f\}
$$

- Joint boolean function $F(X)=\bigwedge c_{S}$


## Applications

Scheduling, rostering, planning, configuration...

## Boolean functions

## SAT and CSP

Excellent to describe, analyze, design perfectly known complex systems

## Boolean functions

## SAT and CSP

Excellent to describe, analyze, design perfectly known complex systems
Biology/Life
Full of imperfectly known complex systems

Cost function network ( $X, W$ ) Joint cost/feasibility distribution ${ }^{3,15}$

- a sequence $X$ of variables $x_{i}$, finite domain $D_{i}$
- a set $W$ of cost functions $w_{\varnothing}$ (Ib)
- $w_{S} \in W$
table/tensor, clause, simple function...

$$
\prod_{i \in S} D_{i} \rightarrow\{0, \ldots, k\}
$$

- Joint cost function $W(X)=\sum w_{S}$
(bounded sum)
Central problems: WCSP (Partial Weighted MaxSAT)
- solution: cost less than $k$
- optimal: w.r.t. the joint cost $W(X)$ decision NP-complete
- constraint: function with costs in $\{0, k\}$ CP is $k=1$


## GMs define

- a joint function of many variables
- by combining (using a dedicated operator)
- a set of simpler functions (scopes, langage)

What function, what query?

- feasibility: prop. logic, constraint nets
(CSP: $\vee, \wedge$ )
- priorities: possibilistic/fuzzy CSP (max, min)
- cost, energy: Cost Function Networks
- probability: Markov Random Field, Bayes nets (Max. a posteriori: $\max , \times$ ) (Marginal:,$+ \times$ )


## Extended most ingredients from SAT/CSP solvers

- Incremental reformulation techniques (tighter lower bound) ${ }^{4}$
- Making assumptions (Hybrid Branch and bound, lb. w $\boldsymbol{w}_{\varnothing}$ )
- Non naive variable ordering (adaptative)
- Graph decomposition (treewidth combined with all the above)
- Dominance analysis (Dead End Elimination)
- Still missing: conflict analysis


## Open source Toulbar2 solver

- Won several competitions (on approximate MAP/MRF solving)
- "ToulBar2 variants were superior to CPLEX variants in all our tests" ${ }^{7}$


## Applications

- Life sciences: protein design, genotyping data diagnosis and repair, RNA gene finding, crop allocation
- NLP, music composition (MLN), Data mining, timetabling, planning, POMDP, universal Hashing based counting, probabilistic inference, Inductive LP, image processing...
- see toulbar2 web site and GitHub


## Most active molecules of life

Sequence of amino acids, 20 natural ones each defined by a specific flexible side-chain


Transporter, binder/regulator, motor, catalyst... Hemoglobine, TAL effector, ATPase, dehydrogenases...

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## Inverse folding

Function



Transporter, binder/regulator, motor, catalyst... Hemoglobine, TAL effector, ATPase, dehydrogenases...

## Why is it worth designing new proteins?

## Eco-friendly chemical/structural nano-agents

- Biodegradable (have been mass produced for billions of year)
- "Easy" to produce (transformed bacteria)
- Useful for health, green chemistry ${ }^{14}$ (biœnergies), nanotechnologies ${ }^{17}$...


## Energy optimisation side - NP-complete

- efficient exact energy optimisation for protein design (far faster than ILP, compete with simulated or D-Wave quantum annealing ${ }^{1116}$ )
- specific extensions for Protein Design: counting, multi-state (flexibility)


## Actual protein designs

- A self assembling hyper-stable protein ${ }^{17}$ (with A. Vœt, KU Leuven)
- New light-weight antibody with nice properties (with A. Olichon, Toulouse Cancer Research Center)

Logical and probabilistic propositional reasoning

- satisfy logical properties/constraints exactly
- optimise a criteria that can be probabilistic (or not)
- which can be learned from data (likelihood/convex optim.).


## Protein Design

- desired design properties (logical information),
- physical knowledge (represented as a decomposable energy function)
- probabilistic information learned from data (known protein sequences)

人-joint project: guaranteed relational probabilistic/logic reasoning Build a rigorous platform (Markov Logic Networks, ${ }^{13}$ Soft Probabilistic Logic, ${ }^{2}$ ProbLog ${ }^{5}$ )

## Topics

- stronger lower bounds: convex/SDP relaxations. $\boldsymbol{\Lambda}$ - PhD .
- learn when to use them, better heuristics (Multi-Armed Bandits, NN).
- extend conflict analysis to CFNs (through duality). $\boldsymbol{\Lambda}$ - PhD
- learn CFNs (available for numerical information)
- parallelization, CPD application, PhDs: \-PostDoc
- Consider multiple protein geometries: Quantified WCSP (bi-level optimisation). ANR SPaceHex.


## Reasoning with rules and data

- Useful for other chairs? (argumentation, NLP, ...)
- Renault and configuration: learning from history (fairness/biases)
- Learning optimally sparse and proving properties of ML models ${ }^{8,12}$
- DL for CPD (adversarial, transformer).


## Continuous optimisation

- Fast incremental convex lower bounds
- Continuous movements: non convex hybrid (discrete/continuous) optimisation problem [6]
- Tight link with robotics (side-chains are robotic arms, J. Cortes/LAAS/CNRS. PhD).


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